

Name: Answer Key TP: \_\_\_\_\_

CW#38H: Two Column Proofs  
Honors Geometry

CRS	Geometry Content
Objective	5.9 Write a two column proof

Think of writing a proof like solving a crime. You survey the crime scene, gather the facts, and write them down in your memo pad. To solve the crime, you take the known facts and, step by step, show who committed the crime. You conscientiously provide supporting evidence for each statement you make. We are not trying to "find an answer", but rather a process for which allows us to prove that something is in fact, true.



First, the blank structure of a proof should look like this:

Given: Known Information	
Prove: Something something	
Statement	Reason
Known Information	Given
-----	-----
(fact #1)	(why the fact #1 is true)
(fact #2)	(why the fact #2 is true)
(fact #...)	(why the fact #... is true)
Something something	
	QED or <input type="checkbox"/>

The proof should *end* with what you are trying to prove

You can end your proof with QED, latin for "Quod erat demonstrandum" which means "Which was needing to be proved" It lets the reader know that something has been definitively proven. You can also draw a box: ☐

Postulate: *statements that are assumed to be true w/out proof (a line contains two points)*

Theorem: *can be proved from definitions, postulates or previously proved theorems (ex- Pythagorean theorem)*

\*Record all postulate and theorems on yellow handout!

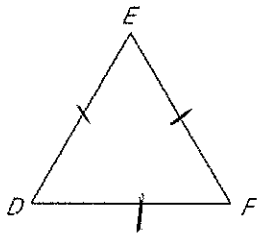
<b>Example 1:</b> <b>GIVEN:</b> $m\angle A = m\angle B$ , $m\angle B = m\angle C$ <b>PROVE:</b> $\angle A \cong \angle C$	
Statements	Reasons
1. $m\angle A = m\angle B$	1. given
2. $m\angle B = m\angle C$	2. given
3. $m\angle A = m\angle C$	3. transitive property
4. $\angle A \cong \angle C$	4. def'n of congruent angles
QED	

PUSH IT TO THE LIMIT.

**Example 2:**

**GIVEN:**  $DE = EF$ ,  $EF = DF$

**PROVE:**  $\overline{DF} \cong \overline{DE}$



Statements	Reasons
1. $\overline{DE} = \overline{EF}$	1. Given
2. $\overline{EF} = \overline{DF}$	2. Given
3. $\overline{DE} = \overline{DF}$	3. Transitive
4. $DF = DE$	4. Symmetric
5. $\overline{DF} \cong \overline{DE}$	5. def'n $\cong$ segments

QED

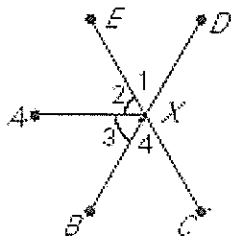
**Example 3:**

**Given**  $m\angle 2 = m\angle 3$ ,

$m\angle AXD =$

$m\angle AXC$

**Prove**  $m\angle 1 = m\angle 4$



Statements	Reasons
1. $m\angle AXC = m\angle AXD$	1. given *write in yellow list
2. $m\angle AXD = m\angle 1 + m\angle 2$	2. angle addition postulate
3. $m\angle AXC = m\angle 3 + m\angle 4$	3. angle addition postulate
4. $m\angle 1 + m\angle 2 = m\angle 3 + m\angle 4$	4. substitution
5. $m\angle 2 = m\angle 3$	5. given
6. $m\angle 1 + m\angle 3 = m\angle 3 + m\angle 4$	6. substitution
7. $m\angle 1 = m\angle 4$	7. subtraction prop of =

QED

1.

**Given**  $BC = AB$

**Prove**  $AC = AB + AB$



Statements	Reasons
1. $BC = AB$	1. Given
2. $AC = AB + BC$	2. Segment addition post.
3. $AC = AB + AB$	3. Substitution

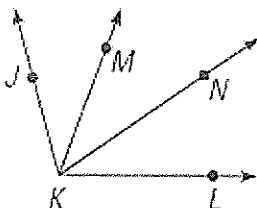
QED

2.

**Given:**  $\overline{KM}$  bisects  $\angle JKN$ ,

$\overline{KN}$  bisects  $\angle MKL$

**Prove:**  $m\angle JKM = m\angle NKL$



Statements	Reasons
① $\overline{KM}$ bisects $\angle JKN$	① Given
② $\angle JKM \cong \angle MKN$	② def'n of angle bisector
③ $\angle MKN \cong \angle NKL$	③ def'n of angle bisector
④ $\angle JKM \cong \angle NKL$	④ transitive prop

**PUSH IT TO THE LIMIT.**

3.

**GIVEN**  $\triangleright \angle 1$  and  $\angle 2$  are supplements.  
 $\angle 3$  and  $\angle 2$  are supplements.

**PROVE**  $\triangleright \angle 1 \cong \angle 3$

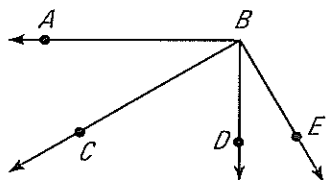


Statements	Reasons
1. $\angle 1$ and $\angle 2$ are supplements. $\angle 3$ and $\angle 2$ are supplements.	1. GIVEN
2. $m\angle 1 + m\angle 2 = 180^\circ$ $m\angle 3 + m\angle 2 = 180^\circ$	2. def'n of supp angles
3. $m\angle 1 + m\angle 2 = m\angle 3 + m\angle 2$	3. substitution
4. $m\angle 1 = m\angle 3$	4. subtraction
5. $\angle 1 \cong \angle 3$	5. def'n of congruent segments

4.

**GIVEN**  $\triangleright \angle ABD$  is a right angle.  
 $\angle CBE$  is a right angle.

**PROVE**  $\triangleright \angle ABC \cong \angle DBE$

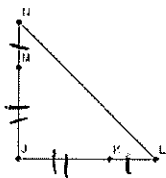


Statements	Reasons
1. $\angle ABD$ is right $\angle$	1. GIVEN
2. $\angle CBE$ is right $\angle$	2. GIVEN
3. $\angle ABC + \angle CBD = \angle ABD$	3. angle addition postulate
4. $\angle CBD + \angle DBE = \angle CBE$	4. angle addition postulate
5. $\angle ABD \cong \angle CBE$	5. def'n congruent angles
6. $\angle ABC + \angle CBD = \angle CBD + \angle DBE$	6. substitution
7. $\angle ABC = \angle DBE$	7. subtraction

5)

**Given:**  $\overline{LK} \cong \overline{NM}$ ,  $\overline{KJ} \cong \overline{MJ}$

**Prove:**  $\overline{LJ} \cong \overline{NJ}$

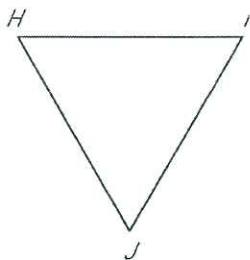


Statements	Reasons
1. $\overline{LK} \cong \overline{NM}$ , $\overline{KJ} \cong \overline{MJ}$	1. given
2. $LK = NM$ $KJ = MJ$	2. Def. of congruent segments
3. $LK + KJ = NM + MJ$	3. addition prop
4. $LK + KJ = LJ$ $NM + MJ = NJ$	4. Segment Addition Postulate
5. $LJ = NJ$	5. substitution
6. $\overline{LJ} \cong \overline{NJ}$	6. def'n congruent segments

Name: \_\_\_\_\_ TP: \_\_\_\_\_

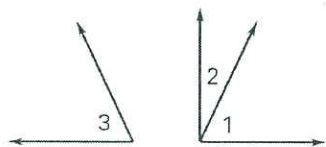
Failure to show work on all problems or use complete sentences will result in a LaSalle.

1. GIVEN:  $HI = 9$ ,  $IJ = 9$ ,  $I\bar{J} \cong J\bar{H}$   
 PROVE:  $H\bar{I} \cong J\bar{H}$



Statements	Reasons
1. $HI = 9$	1. given
2. $IJ = 9$	2. given
3. $HI \cong IJ$	3. substitution
4. $H\bar{I} \cong I\bar{J}$	4. def'n $\cong$ seg
5. $I\bar{J} \cong J\bar{H}$	5. given
6. $H\bar{I} \cong J\bar{H}$	6. transitive

2. GIVEN:  $\angle 3$  and  $\angle 2$  are complementary.  
 $m\angle 1 + m\angle 2 = 90^\circ$

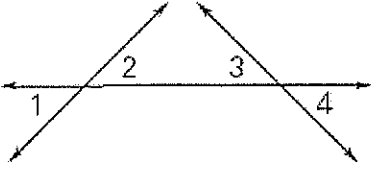
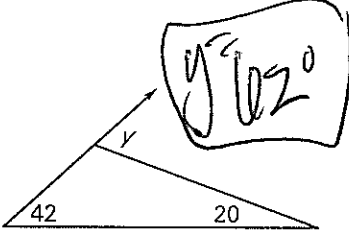
PROVE:  $\angle 3 \cong \angle 1$ 

Statements	Reasons
1. $\angle 3$ and $\angle 2$ are complementary	1. given
2. $m\angle 1 + m\angle 2 = 90^\circ$	2. given
3. $m\angle 3 + m\angle 2 = 90^\circ$	3. def'n comp $\angle$ 's
4. $m\angle 1 + m\angle 2 = m\angle 3 + m\angle 2$	4. substitution
5. $m\angle 1 = m\angle 3$	5. subtraction
6. $\angle 1 \cong \angle 3$	6. def'n cong. angles

3. GIVEN:  $AL = SK$   
 PROVE:  $AS = LK$

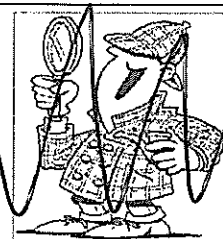


Statements	Reasons
1. $AL = SK$	1. given
2. $LS = LS$	2. reflexive
3. $AL + LS = SK + LS$	3. add prop of $=$
4. $AL + LS = AS$	4. seg + post
5. $SK + LS = LK$	5. seg + post
6. $AS = LK$	6. substitution

<p>4.</p> <p>GIVEN: <math>\angle 2 \cong \angle 3</math></p> <p>PROVE: <math>\angle 1 \cong \angle 4</math></p> 	<table border="1"> <thead> <tr> <th>Statements</th><th>Reasons</th></tr> </thead> <tbody> <tr> <td>1. <math>\angle 2 \cong \angle 3</math></td><td>1. given</td></tr> <tr> <td>2. <math>\angle 3 \cong \angle 4</math></td><td>2. vertical angles</td></tr> <tr> <td>3. <math>\angle 2 \cong \angle 4</math></td><td>3. transitive</td></tr> <tr> <td>4. <math>\angle 1 \cong \angle 2</math></td><td>4. vertical</td></tr> <tr> <td>5. <math>\angle 1 \cong \angle 4</math></td><td>5. transitive</td></tr> </tbody> </table>	Statements	Reasons	1. $\angle 2 \cong \angle 3$	1. given	2. $\angle 3 \cong \angle 4$	2. vertical angles	3. $\angle 2 \cong \angle 4$	3. transitive	4. $\angle 1 \cong \angle 2$	4. vertical	5. $\angle 1 \cong \angle 4$	5. transitive
Statements	Reasons												
1. $\angle 2 \cong \angle 3$	1. given												
2. $\angle 3 \cong \angle 4$	2. vertical angles												
3. $\angle 2 \cong \angle 4$	3. transitive												
4. $\angle 1 \cong \angle 2$	4. vertical												
5. $\angle 1 \cong \angle 4$	5. transitive												
<p>5. At what point does the line <math>y = -2x + 2</math> cross the x-axis?</p> <p><math>y=0</math></p> <p><math>0 = -2x + 2</math></p> <p><math>-2 = -2x</math></p> <p><math>x=1</math></p> <p><math>(1,0)</math></p>	<p>6. Solve for x in the following equation:</p> $y = x^2 + 3w$ $\sqrt{y-3w} = x$												
<p>7. What are the roots of the equation <math>x^2 - 3x = 18</math>?</p> <p><math>x^2 - 3x - 18</math></p> <p><math>(x+3)(x-6)</math></p> <p><math>x = -3, 6</math></p>	<p>8. <math>x = \{-2, 4\}</math> is a solution set for what quadratic equation?</p> <p><math>(x+2)(x-4)</math></p> <p><math>x^2 - 2x - 8</math></p>												
<p>9. A circle has a circumference of <math>10\pi</math> centimeters. What is the area of that circle, in terms of <math>\pi</math>?</p> <p><math>C = 10\pi</math></p> <p><math>d = 10</math></p> <p><math>r = 5</math></p> <p><math>A = 25\pi \text{ cm}^2</math></p>	<p>10. Find the value of y in the figure below:</p>  <p><math>y = 102^\circ</math></p>												

CRS	Geometry Content
Objective	5.9 Write a two column proof
Critical Thinking	Reasoning and Argumentation: Construct well-reasoned arguments or proofs to explain issues; Address challenges by providing a logical explanation or refutation, or by acknowledging the accuracy of the challenge

Think of writing a proof like solving a crime. You survey the crime scene, gather the facts, and write them down in your memo pad. To solve the crime, you take the known facts and, step by step, show who committed the crime. You conscientiously provide supporting evidence for each statement you make. We are not trying to "find an answer", but rather a process for which allows us to prove that something is in fact, true.

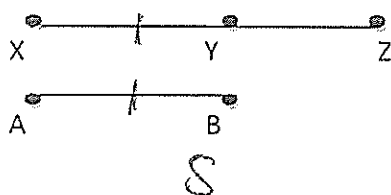


### SUBSTITUTION

#### EXAMPLE 1:

Given:  $XY = AB$

Prove:  $AB + YZ = XZ$



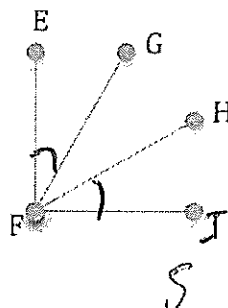
- ①  $XY = AB$   
②  $XZ = XY + YZ$   
③  $XZ = AB + YZ$

- ① given  
② segment + postulate  
③ substitution

#### EXAMPLE 2:

Given:  $\angle EFG \cong \angle HFI$

Prove:  $\angle EFH \cong \angle GFH + \angle HFI$



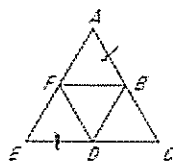
- ①  $\angle EFG \cong \angle HFI$   
②  $\angle EFH = \angle EFG + \angle GFH$   
③  $\angle EFH = \angle HFI + \angle GFH$

- ① given  
② angle addition postulate  
③ substitution

1.

Given:  $ED = AB$

Prove:  $EC = AB + DC$



- ①  $ED = AB$   
②  $EC = ED + DC$   
③  $EC = AB + DC$

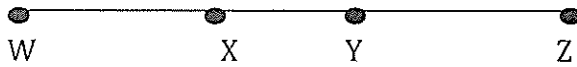
- ① given  
② segment addition post.  
③ substitution

# ADDITION

## EXAMPLE 3:

Given:  $WX \cong YZ$

Prove:  $WY \cong XZ$



S

R

1)  $WX \cong YZ$

2)  $XY \cong XY$

3)  $WX + XY \cong YZ + XY$

4)  $WY = WX + XY$

$XZ = XY + YZ$

5)  $WY \cong XZ$

1) Given

2) Reflexive

3) add. prop. of =

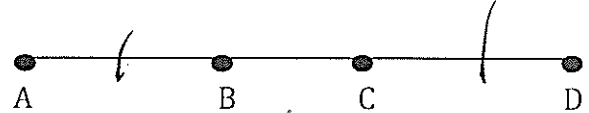
4) segment add. post.

5) substitution

2.

Given:  $AB \cong CD$

Prove:  $AC \cong BD$



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R

1)  $AB \cong CD$

2)  $BC \cong BC$

3)  $AB + BC \cong CD + BC$

4)  $AC = AB + BC$

$BD = BC + CD$

5)  $AC \cong BD$

1) Given

2) Reflexive

3) add. prop

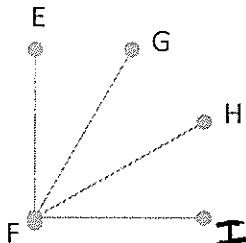
4) segment add. prop.

5) substitution

## EXAMPLE 4:

Given:  $\angle EFG \cong \angle HFI$

Prove:  $\angle EFH \cong \angle GFI$



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R

1)  $\angle EFG \cong \angle HFI$

2)  $\angle GFH \cong \angle GFH$

3)  $\angle EFG + \angle GFH = \angle HFI + \angle GFH$

4)  $\angle EFH = \angle EFG + \angle GFH$

$\angle GFI = \angle GFH + \angle HFI$

5)  $\angle EFH \cong \angle GFI$

1) Given

2) Reflexive

3) add. prop. of =

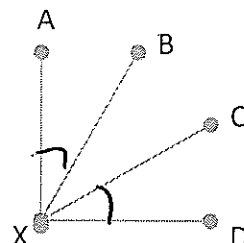
4) angle addition postulate

5) substitution

3.

Given:  $\angle AXB \cong \angle CXD$

Prove:  $\angle AXC \cong \angle BXD$



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1)  $\angle AXB \cong \angle CXD$

2)  $\angle BXC \cong \angle BXC$

3)  $\angle AXB + \angle BXC = \angle CXD + \angle BXC$

4)  $\angle AXC = \angle AXB + \angle BXC$

$\angle BXD = \angle BXC + \angle CXD$

5)  $\angle AXC \cong \angle BXD$

1) Given

2) Reflexive

3) add. prop

4) angle add.

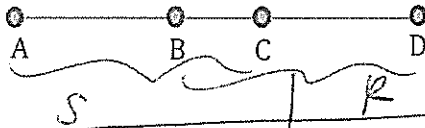
5) substitution

# SUBTRACTION

## EXAMPLE 5:

Given:  $AC = BD$

Prove:  $AB = CD$

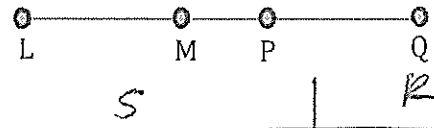


- |   |   |
|---|---|
| <p>① <math>AC = BD</math></p> <p>② <math>BC = BC</math></p> <p>③ <math>AC = AB + BC</math></p> <p>④ <math>BD = BC + CD</math></p> <p>⑤ <math>AB + BC = BC + CD</math><br/> <math>\quad \quad \quad -BC \quad -BC</math></p> <p>⑥ <math>AB = CD</math></p> | <p>① given</p> <p>② reflexive</p> <p>③ segment addition postulate</p> <p>④ substitution</p> <p>⑤ subtraction property of <math>=</math></p> |
|---|---|

4.

Given:  $LP = MQ$

Prove:  $LM = PQ$



- |   |   |
|---|---|
| <p>① <math>LP = MQ</math></p> <p>② <math>MP = MP</math></p> <p>③ <math>LP = LM + MP</math></p> <p>④ <math>MQ = MP + PQ</math></p> <p>⑤ <math>LM + MP = MP + PQ</math><br/> <math>\quad \quad \quad -MP \quad -MP</math></p> <p>⑥ <math>LM = PQ</math></p> | <p>① given</p> <p>② reflexive</p> <p>③ segment addition postulate</p> <p>④ substitution</p> <p>⑤ subtraction property of <math>=</math></p> |
|---|---|

# TRANSITIVE (& SYMMETRIC)

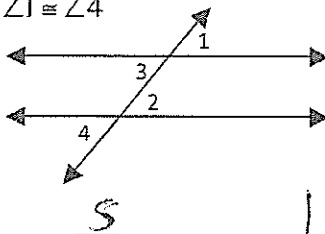
## EXAMPLE 6:

Given:  $\angle 1 \cong \angle 3$

$\angle 3 \cong \angle 2$

$\angle 2 \cong \angle 4$

Prove:  $\angle 1 \cong \angle 4$



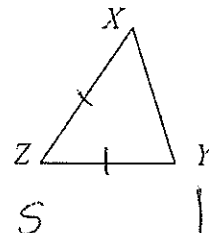
- |   |   |
|---|---|
| <p>① <math>\angle 1 \cong \angle 3, \angle 3 \cong \angle 2</math><br/> <del><math>\angle 1 \cong \angle 2</math></del></p> <p>② <math>\angle 1 \cong \angle 2</math></p> <p>③ <math>\angle 2 \cong \angle 4</math></p> <p>④ <math>\angle 1 \cong \angle 4</math></p> | <p>① given</p> <p>② transitive</p> <p>③ given</p> <p>④ transitive</p> |
|---|---|

5.

Given:  $XZ \cong ZY$

$ZY \cong YX$

Prove:  $XZ \cong YX$



- |  |                                    |
|--|------------------------------------|
| <p>① <math>XZ \cong ZY, ZY \cong YX</math></p> <p>② <math>XZ \cong YX</math></p> | <p>① given</p> <p>② transitive</p> |
|--|------------------------------------|

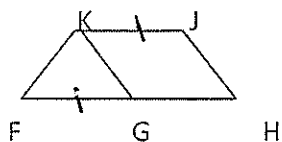


EXAMPLE 7: \*TRANSITIVE WILL NOT ALWAYS BE IN ORDER!

Given:  $FG \cong KJ$

$GH \cong KJ$

Prove:  $FG \cong GH$



S

R

①  $FG \cong KJ$   $GH \cong KJ$

① given

②  $KJ \cong GH$

② symmetric

③  $FG \cong GH$

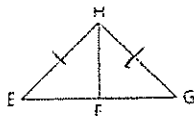
③ transitive

6.

Given:  $HE \cong HG$

$FG \cong HG$

Prove:  $HE \cong FG$



S

R

①  $HE \cong HG$   $FG \cong HG$

① given

②  $HG \cong FG$

② symmetric

③  $HE \cong FG$

③ transitive

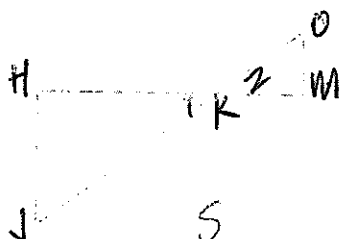
VERTICAL ANGLES

PERPENDICULARITY

EXAMPLE 8:

Given:  $\angle J \cong \angle I$

Prove:  $\angle J \cong \angle 2$



S

R

①  $\angle J \cong \angle I$

① given

②  $\angle I \cong \angle 2$

② vertical angles

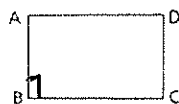
③  $\angle J \cong \angle 2$

③ transitive

EXAMPLE 9:

Given:  $\overline{AB} \perp \overline{BC}$ ,  $\overline{DC} \perp \overline{BC}$

Prove:  $\angle B \cong \angle C$



S

R

①  $AB \perp BC$

① given

②  $\angle B$  is a right angle

② def'n of  $\perp$  lines

③  $DC \perp BC$

③ given

④  $\angle C$  is a right  $\angle$

④ def'n  $\perp$  lines

⑤  $\angle B \cong \angle C$

⑤ def'n  $\cong$  angles

Name: ANSWER KEY TP: \_\_\_\_\_

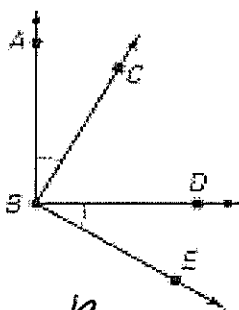
HW#39H: Two Column Proofs  
Honors Geometry  
Due Date: Wednesday, Nov. 14<sup>th</sup>, 2012

Failure to show work on all problems or use complete sentences will result in a LaSalle.

1) Use the Addition Property

Given:  $\angle ABC \cong \angle DBE$

Prove:  $\angle ABD \cong \angle CBE$

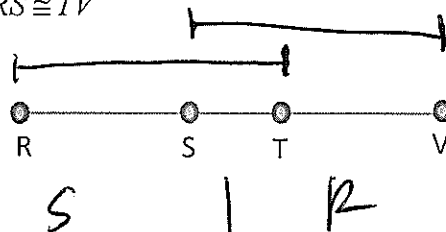


S	R
1.) $\angle ABC \cong \angle DBE$	1.) Given
2.) $\angle CBD \cong \angle CBD$	2.) Reflexive
3.) $\angle ABC + \angle CBD = \angle DBE + \angle CBD$	3.) <del>add</del> add prop if =
4.) $\angle ABD = \angle ABC + \angle CBD$ $\angle CBE = \angle CBD + \angle DBE$	4.) add addition prop
5.) $\angle ABD \cong \angle CBE$	5.) substitution

2) Use the Subtraction Property

Given:  $RT \cong SV$

Prove:  $RS \cong TV$



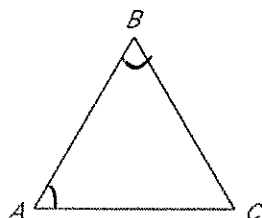
S	R
1.) $RT \cong SV$	1.) Given
2.) $ST \cong ST$	2.) Reflexive
3.) $RT = RS + ST$ $SV = ST + TV$	3.) seg. + post.
4.) $RS + ST = ST + TV$ $ST - ST$	4.) substitution
5.) $RS = TV$	5.) subtraction

3) Use the Transitive Property

GIVEN:  $m\angle A = m\angle B$

$m\angle C = m\angle B$

PROVE:  $\angle A \cong \angle C$

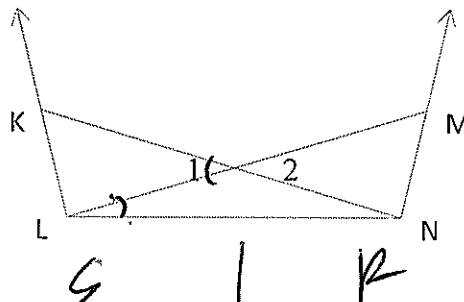


S	R
1.) $m\angle A = m\angle B$	1.) Given
2.) $m\angle C = m\angle B$	2.) Given
3.) $m\angle B \cong m\angle C$	3.) Symmetric
4.) $m\angle A = m\angle C$	4.) transitive

4) Use Vertical Angles

Given:  $\angle MLN \cong \angle 1$

Prove:  $\angle MLN \cong \angle 2$

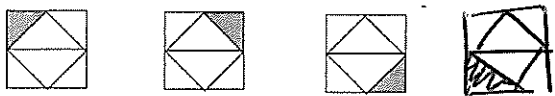


S	R
1.) $\angle MLN \cong \angle 1$	1.) Given
2.) $\angle 1 \cong \angle 2$	2.) vertical angles
3.) $m\angle MLN = m\angle 2$	3.) transitive

PUSH IT TO THE LIMIT.

## QUIZ REVIEW!

5) Is the following an example of inductive or deductive reasoning? Determine the next figure.



inductive

6) Is the following an example of inductive or deductive reasoning? Explain.

All athletes work out in the gym. Barry Bonds is an athlete. Therefore, Barry Bonds works out in the gym.

deductive

Two adjacent angles are a linear pair.

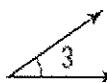
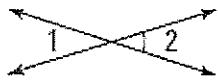
True/False

7) Conditional Statement	If two angles are adjacent, then they are a linear pair	F
Converse	If two angles are a linear pair, then they are adjacent	T
Inverse	If two angles are not adj, then are not linear pair	T
Contrapositive	If two angles are not a linear pair, then they are not adjacent	F

8)

$\angle 1$  and  $\angle 2$  are vertical angles, and  $\angle 2 \cong \angle 3$ .

Show that  $\angle 1 \cong \angle 3$ .



$$\angle 1 \cong \angle 2$$

vertical angles theorem

$$\angle 2 \cong \angle 3$$

Given

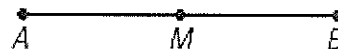
$$\angle 1 \cong \angle 3$$

transitive

Property of Congruence

9) In the diagram,  $M$  is the midpoint of  $\overline{AB}$ .

Show that  $AB = 2 \cdot AM$ .



$$MB = AM$$

Definition of midpoint

$$AB = AM + MB$$

Segment Addition Postulate

$$AB = AM + AM$$

substitution Property of Equality

$$AB = 2 \cdot AM$$

Distributive property

10)

Name the property that the statement illustrates.

1. If  $DF = FG$  and  $FG = GH$ , then  $DF = GH$  transitive

2.  $\angle P \cong \angle P$  reflexive

3. If  $m\angle S = m\angle T$ , then  $m\angle T = m\angle S$  symmetric

11) Solve  $5(x - 4) = 3x + 2$ . Write a reason for each step.

$$\begin{aligned} 5(x - 4) &= 3x + 2 && \text{S} \\ 5x - 20 &= 3x + 2 && \\ 5x - 20 &= 3x + 2 && \\ 2x - 20 &= 2 && \\ 2x - 20 &= 2 && \\ x &= 11 && \end{aligned}$$

given  
dist  
subt  
add  
division